

# Analog - Adjustable Sallen and Key Low-Pass Filters

# AN2031

Authors: Dennis Seguine and Casey McNeese Associated Project: No Associated Part Family: CY8C25xxx, CY8C26xxx GET FREE SAMPLES HERE Software Version: NA Associated Application Notes: None

## Application Note Abstract

Sallen and Key low-pass filters are constructed using continuous time (CT) analog PSoC® blocks. Methods are shown for making the filters adjustable for use as audio-tone control.

# Introduction

The PSoC device has switched capacitor (SC) analog blocks that can be used to form filters of most common types. However, these may not always be suitable for all filter needs. In this case, the continuous time analog blocks can be utilized to form standard classes of analog filters.

# The Need for Non-SC Filters

PSoC SC filter User Modules have characteristics that are determined by the ratios of capacitor values in the selected blocks and the clock frequency driving the blocks. These filters are useful at frequencies up to the Nyquist rate, or half of the sampling frequency.

The highest ratio of sampling frequency to filter nominal corner frequency (over sample ratio, or OSR) is limited by available capacitor ratios to approximately 160. Thus, the maximum usable frequency for a low-pass filter is 80 times the corner frequency. There may be a need for attenuation of noise and spurious signals at frequencies above this range; or, the system design may have simply consumed all SC blocks and an anti-aliasing filter is still needed. Accordingly, we need another way to make the low-pass filter.

# **Low-Pass Filter Transfer Function**

The frequency performance of the two-pole, low- pass filter is described by the transfer function:

$$\frac{Vout}{Vin} = \frac{K\omega_n^2 \omega_0^2}{s^2 + sd\omega_n \omega_0 + \omega_n^2 \omega_0^2}$$

Where:

- $\omega_0$  = nominal corner frequency
- $\omega_n$  = normalized corner frequency ( $2\pi f_c$ )
- d = damping factor.

 $\omega_0$  and *d* for standard filter implementations are calculated from the complex pole locations for the specific filter to be implemented. The complex pole locations  $(\alpha + j\beta)$  for a low-pass filter are converted to  $\omega_0$  and *d*.

$$\omega_0 = \sqrt{\alpha^2 + \beta^2} \quad d = \frac{2\alpha}{\omega_0}$$

A design example is shown for a Butterworth filter. The transfer function for the Butterworth has  $\omega_0 = 1.0$  and d = 1.414. Filters other than Butterworth will have  $\omega_0$  shifted from 1.0. Filters with flatter in-band response, such as Chebychev, have lower damping and slightly lower  $\omega_0$ . Pole locations, or  $\omega_0$  and d, are readily available from any number of filter references<sup>1</sup>.

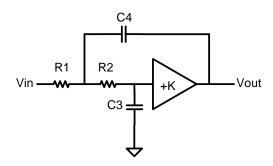
<sup>&</sup>lt;sup>1</sup> <u>Electronic Filter Design Handbook</u>, Arthur B. Williams and Fred J. Taylor, McGraw-Hill, 1981, Tables in Chapter 11.

### Sallen and Key Low-Pass Filters

The Sallen and Key<sup>2</sup> filter implementation is the simplest active filter. It uses the lowest number of components and the design equations are relatively straightforward. It has been discussed, reviewed, and analyzed in great depth in hundreds of published articles, reference texts, design handbooks<sup>3</sup> and at great length on the web since the original Sallen and Key paper in the IRE in 1955. This form is often preferred to the biquad and multiple-loop feedback approaches because it does not invert the signal.

The simplest form of the Sallen and Key implementation of the two-pole, low-pass filter is shown in Figure 1. Multiple pole-pair filters are easily implemented by cascading filter sections.

Figure 1. Schematic Low-Pass Filter



\*\*

The circuit has the transfer function:

$$\frac{Vout}{Vin} = \frac{\frac{K}{R_1 R_2 C_3 C_4}}{s^2 + s \left(\frac{1-K}{R_2 C_3} + \frac{R_1 + R_2}{R_2 R_2 C_4}\right) + \frac{1}{R_1 R_2 C_3 C_4}}$$

From this, we derive design equations:

$$R_{1} = \frac{d + \sqrt{d^{2} - 4(C_{3}/C_{4} + 1 - K)}}{2\omega_{0}\omega_{n}(C_{3} + (1 - K)C_{4})}$$
$$R_{2} = \frac{1}{R_{1}C_{3}C_{4}(\omega_{0}\omega_{n})^{2}}$$

C3 can be arbitrarily chosen to meet the impedance requirements of the circuit.

C4 must be chosen to meet the requirement:

$$d^{2} - 4(C_{3}/C_{4} + 1 - K) \ge 0$$
  
or  $C_{4} \ge \frac{C_{3}}{d^{2}/4 - 1 + K}$ 

In the simplest case, setting the low-pass gain, K, to 1.00 vields a further simplification of the calculation of C4:

$$C_4 \ge \frac{4C_3}{d^2}$$

Once the value for C4 has been established, finding R1 and R2 is a simple calculation.

### 1. PSoC Design Example

A design example is demonstrated for two-pole, low-pass Butterworth at 1000 Hz. In this case:

$$d = 1.414$$
  

$$\omega_{0} = 1.00$$
  

$$\omega_{n} = 2\pi 1000$$
  

$$K = 1.00$$
  
Let  $C_{3} = 0.001 \mu F$   

$$C_{4} \ge \frac{4 \cdot 0.001 \mu F}{1.414^{2}} \ge .002 \mu F$$
  
Let  $C_{4} = 0.0022 \mu F$   
 $(1 - K) = 0$   
so...

S

$$R_{1} = \frac{d + \sqrt{d^{2} - 4(\frac{C_{3}}{C_{4}})}}{2(C_{3} + C_{4}(0))\omega_{0}\omega_{n}}$$

$$R_{1} = \frac{1.414 + 1.414}{2 * 0.001 uF * 1.0 * 2\pi 1000} = 146.5k\Omega$$

$$R_{2} = \frac{1}{146.5k\Omega(.001 uF)(.0022 uF)} = 78.67k\Omega$$

The result is a filter that follows the canonical form for the two-pole, low-pass Butterworth filter.

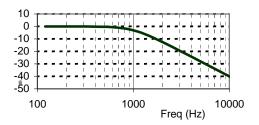
2

<sup>&</sup>lt;sup>2</sup> Sallen, R.P. "A Practical Method of Designing RC Active Filters," IRE Transactions Circuit Theory, Vol CT-2, March 1955, pp74-85.

Active Filter Cookbook, Don Lancaster, Howard W. Sams & Co., 1975.

#### Figure 2. 1000 Hz Low-Pass Filter

#### 2 Pole Low Pass Filter



Accuracy of the filter is limited primarily by the accuracy of the selected passive components.

### **PSoC Implementation**

The gain stage (K) for the filter is a continuous time (CT) Programmable Gain Amplifier (PGA) User Module selectable in PSoC Designer.

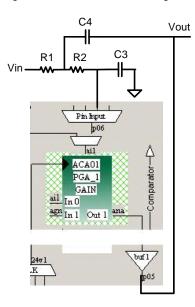


Figure 3. Low-Pass Filter Using PGA

The PGA output is enabled onto the Analog Output Bus for the column. The Analog Output Bus drives an analog buffer, which is connected to an output on Port 0. This port output drives feedback capacitor, C4. C3 should be connected to analog ground. There are several selections for this connection:

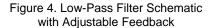
- User-provided external ground, or
- Buffered analog ground, generated from AGND signal in the CT block and passed through that blocks' TestMux to another analog buffer, or
- Resistive divider from V<sub>cc</sub> to V<sub>ss</sub>, where both resistors are 2.0 times the nominal value for R2.

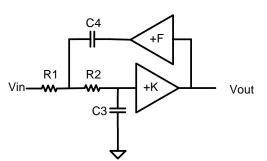
The resulting output in all cases is referenced to the selected PSoC analog ground.

This combination of the PGA and the analog buffer has sufficient gain-bandwidth to provide accurate low-pass filters of audio signals. This filter functions well for roll-off frequencies up to one tenth the gain bandwidth of the amplifier. The power level for PGA should be set to match the upper-end bandwidth requirements of the filter.

### Adjustable Low-Pass Filter

A simple modification to the filter block diagram allows a degree of flexibility. The addition of a feedback gain amplifier is shown:





The transfer function is only slightly more complex, and the design equations are identical for feedback gain, F=1.00.

$$\frac{Vout}{Vin} = \frac{\frac{FK}{R_1R_2C_3C_4}}{s^2 + s\left(\frac{1 - FK}{R_2C_3} + \frac{R_1 + R_2}{R_1R_2C_4}\right) + \frac{1}{R_1R_2C_3C_4}}$$

The transfer function is valid as long as:

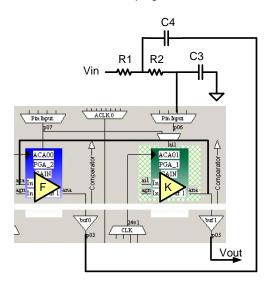
$$\left(\frac{1-FK}{R_2C_3} + \frac{R_1 + R_2}{R_1R_2C_4}\right) > 0$$

When this term goes negative, the poles shift from complex conjugate pair, with both having negative real part, to a pair of real poles, but with one pole having positive real part. This is, of course, an oscillator.

### 2. PSoC Design Example

We build on the structure of the earlier example to configure the adjustable filter. The design equations are the same, but an additional PGA is shown to implement the feedback gain, F.

Figure 5: Low-Pass Filter with Second PGA for Adjustable Damping

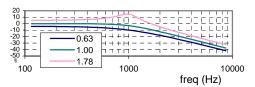


The output of PGA K (in ACA01) is routed in the PSoC connections to the input of the adjacent PGA (in ACA00) to form the feedback amplifier, F. The output of F is connected to its Analog Output Bus and the analog buffer is enabled. The output of this buffer drives R4. The output of PGA K does not need to be connected to its Analog Output Bus unless it is required for test purposes to bring the signal off-chip. The output of PGA K can be directly connected to a PGA in an adjacent CT block (ACA02 in this example), the input of a switched capacitor (SC) low-pass filter (LPF2), SC band-pass filter (BPF2), or analog to-digital converter.

Using the 150 Hz Butterworth example as before, we show the range of control in damping factor as a function of feedback gain.

Figure 6: 150 Hz Low-Pass Filter Adjustable Damping

#### Adjustable LPF



The lower limit of feedback gain is the 0.063 setting of the gain for PGA F. The upper limit for feedback gain is determined by transfer function requirements as discussed earlier. This configuration allows adjustment of the response at the nominal corner frequency over a range from -6 to +12 dB. This range is useful for audio-tone controls or dynamic adjustment of closed-loop, feedback-control transfer function.

The feedback gain can be adjusted "on-the-fly" using the SetGain\_xxx commands in the API for the PGA F User Module.

A simple spreadsheet for the design of this filter is included in the documentation section of PSoC Designer, releases 3.0 and later.

### Summary

Complete design methodology has been demonstrated for building Sallen and Key low-pass filters using the analog capabilities of the PSoC device. In March of 2007, Cypress recataloged all of its Application Notes using a new documentation number and revision code. This new documentation number and revision code (001-xxxxx, beginning with rev. \*\*), located in the footer of the document, will be used in all subsequent revisions.

PSoC is a registered trademark of Cypress Semiconductor Corp. "Programmable System-on-Chip," PSoC Designer, and PSoC Express are trademarks of Cypress Semiconductor Corp. All other trademarks or registered trademarks referenced herein are the property of their respective owners.

Cypress Semiconductor 198 Champion Court San Jose, CA 95134-1709 Phone: 408-943-2600 Fax: 408-943-4730 http://www.cypress.com/

© Cypress Semiconductor Corporation, 2002-2007. The information contained herein is subject to change without notice. Cypress Semiconductor Corporation assumes no responsibility for the use of any circuitry other than circuitry embodied in a Cypress product. Nor does it convey or imply any license under patent or other rights. Cypress products are not warranted nor intended to be used for medical, life support, life saving, critical control or safety applications, unless pursuant to an express written agreement with Cypress. Furthermore, Cypress does not authorize its products for use as critical components in life-support systems where a malfunction or failure may reasonably be expected to result in significant injury to the user. The inclusion of Cypress products in life-support systems application implies that the manufacturer assumes all risk of such use and in doing so indemnifies Cypress against all charges.

This Source Code (software and/or firmware) is owned by Cypress Semiconductor Corporation (Cypress) and is protected by and subject to worldwide patent protection (United States and foreign), United States copyright laws and international treaty provisions. Cypress hereby grants to licensee a personal, non-exclusive, non-transferable license to copy, use, modify, create derivative works of, and compile the Cypress Source Code and derivative works for the sole purpose of creating custom software and or firmware in support of licensee product to be used only in conjunction with a Cypress integrated circuit as specified in the applicable agreement. Any reproduction, modification, translation, compilation, or representation of this Source Code except as specified above is prohibited without the express written permission of Cypress.

Disclaimer: CYPRESS MAKES NO WARRANTY OF ANY KIND, EXPRESS OR IMPLIED, WITH REGARD TO THIS MATERIAL, INCLUDING, BUT NOT LIMITED TO, THE IMPLIED WARRANTIES OF MERCHANTABILITY AND FITNESS FOR A PARTICULAR PURPOSE. Cypress reserves the right to make changes without further notice to the materials described herein. Cypress does not assume any liability arising out of the application or use of any product or circuit described herein. Cypress does not authorize its products for use as critical components in life-support systems where a malfunction or failure may reasonably be expected to result in significant injury to the user. The inclusion of Cypress' product in a life-support systems application implies that the manufacturer assumes all risk of such use and in doing so indemnifies Cypress against all charges.

Use may be limited by and subject to the applicable Cypress software license agreement.